

Intermediate Algebra

Skill-Builder # AE - 7

Writing a Polynomial Multiplication Problem as a Binomial Multiplication Problem

Strategy: Use either shapes or letters to reduce the multiplication problem to one of the following forms and apply the corresponding formula:

$$(\text{Binomial A})(\text{Binomial B}) \quad (\boxed{} + \bigcirc)(\diamond + \boxed{}) = \boxed{}\diamond + \boxed{}\boxed{} + \bigcirc\diamond + \bigcirc\boxed{}$$

$$(\text{Binomial A } +)(\text{Binomial A } -) \quad (\boxed{} + \bigcirc)(\boxed{} - \bigcirc) = \boxed{}^2 - \bigcirc^2$$

$$\text{Square of Binomial } + \quad (\boxed{} + \bigcirc)^2 = \boxed{}^2 + 2\boxed{}\bigcirc + \bigcirc^2$$

$$\text{Square of Binomial } - \quad (\boxed{} - \bigcirc)^2 = \boxed{}^2 - 2\boxed{}\bigcirc + \bigcirc^2$$

Examples

$$1. [(x+1)-y][(x+1)+y] = [\boxed{x+1} - \bigcirc][\boxed{x+1} + \bigcirc] = \boxed{x+1}^2 - \bigcirc^2$$

$$2. [(a+3)+b][c+(d-1)] = [\boxed{a+3} + \bigcirc][\diamond + \boxed{d-1}] = \boxed{a+3}\diamond + \boxed{a+3}\boxed{d-1} + \bigcirc\diamond + \bigcirc\boxed{d-1}$$

$$3. [n+(m-p)]^2 = [\boxed{n} + \bigcirc(m-p)]^2 = \boxed{n}^2 + 2\boxed{n}\bigcirc(m-p) + \bigcirc(m-p)^2$$

$$4. [(y+4)-(x-5)]^2 = [\boxed{y+4} - \bigcirc(x-5)]^2 = \boxed{y+4}^2 - 2\boxed{y+4}\bigcirc(x-5) + \bigcirc(x-5)^2$$

One can also use letters:

$$1. \left[\underbrace{(x+1)}_a - y \right] \left[\underbrace{(x+1)}_a + y \right] = (a-y)(a+y) = a^2 - y^2 = (x+1)^2 - y^2$$

$$2. \left[\underbrace{(a+3)}_x + b \right] \left[c + \underbrace{(d-1)}_y \right] = (x+b)(c+y) = xc + xy + bc + by = (a+3)c + (a+3)y + bc + b(d-1)$$

$$3. \left[n + \underbrace{(m-p)}_x \right]^2 = (n+x)^2 = n^2 + 2nx + x^2 = n^2 + 2n(m-p) + (m-p)^2$$

$$4. \left[\underbrace{(y+4)}_a - \underbrace{(x-5)}_b \right]^2 = (a-b)^2 = a^2 - 2ab + b^2 = (y+4)^2 - 2(y+4)(x-5) + (x-5)^2$$

Intermediate Algebra**Skill-BUILDER # AE - 7****Writing a Polynomial Multiplication Problem as a Binomial Multiplication Problem**

Use either shapes or letters to rewrite the given multiplication problem as a binomial multiplication problem.

1. $[a-(b+2)]^2$

2. $[(x+y)+4n][(x+y)-4n]$

3. $[(n-1)+2m][(n+1)-3m]$

4. $[(b-2)-(a-c)]^2$

5. $[x+(2y-1)][(x+1)-5y]$

6. $[(p+q)-(r+s)][(p+q)+(r+s)]$

7. $[4y+(x-1)]^2$

8. $[(2a-b)-(3c+4d)]^2$

Intermediate Algebra**Skill-BUILDER # AE - 7****Writing a Polynomial Multiplication Problem as a Binomial Multiplication Problem****Answers**

Using letters:

1. $(x - y)^2$

2. $(a + b)(a - b)$

3. $(a + b)(c - d)$

4. $(x - y)^2$

5. $(a + b)(c - d)$

6. $(a + b)(a - b)$

7. $(a + b)^2$

8. $(x - y)^2$

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